

Pravila diferenciranja

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$$1) (C u)' = C u'$$

$$2) (u + v)' = u' + v'$$

$$3) (u - v)' = u' - v'$$

$$4) (u \cdot v)' = u' \cdot v + u \cdot v'$$

$$5) \left(\frac{u}{v} \right)' = \frac{u' \cdot v - u \cdot v'}{v^2}$$

Tablica izvoda nekih elementarnih funkcija

$(C)' = 0, C - \text{const.}$	$(e^x)' = e^x$	$(a^x)' = a^x \ln a$
$(x^n)' = nx^{n-1}, n \in R$	$(\sin x)' = \cos x$	$(\arcsin x)' = \frac{1}{\sqrt{1-x^2}}$
$\left(\frac{1}{x}\right)' = -\frac{1}{x^2}, (\sqrt{x})' = \frac{1}{2\sqrt{x}}$	$(\cos x)' = -\sin x$	$(\arccos x)' = -\frac{1}{\sqrt{1-x^2}}$
$(\log_a x)' = \frac{1}{x \cdot \ln a}$	$(\operatorname{tg} x)' = \frac{1}{\cos^2 x}$	$(\operatorname{arctg} x)' = \frac{1}{1+x^2}$
$(\ln x)' = \frac{1}{x}, x \in R/\{0\}$	$(\operatorname{ctg} x)' = -\frac{1}{\sin^2 x}$	$(\operatorname{arcctg} x)' = -\frac{1}{1+x^2}$

Primjer 1. Odrediti izvode sledećih funkcija:

$$a) y = 3x^3 - 4x^2 + 2x$$

$$y' = 3 \cdot 3x^{3-1} - 4 \cdot 2x^{2-1} + 2 \cdot 1x^{1-1}$$

$$y' = 9x^2 - 8x^1 + 2x^0$$

$$y' = 9x^2 - 8x + 2$$

$$(x^n)' = nx^{n-1}$$

$$b) y = (3x^2 + 1) \cdot (2x^2 + 3)$$

$$(u \cdot v)' = u' \cdot v + u \cdot v'$$

$$y' = (3x^2 + 1)' \cdot (2x^2 + 3) + (3x^2 + 1) \cdot (2x^2 + 3)'$$

$$y' = (3 \cdot 2x^{2-1} + 0) \cdot (2x^2 + 3) + (3x^2 + 1) \cdot (2 \cdot 2x^{2-1} + 0)$$

$$y' = 6x \cdot (2x^2 + 3) + (3x^2 + 1) \cdot 4x$$

$$y' = 6x \cdot 2x^2 + 6x \cdot 3 + 3x^2 \cdot 4x + 1 \cdot 4x$$

$$y' = 12x^3 + 18x + 12x^3 + 4x = (12x^3 + 12x^3) + (18x + 4x)$$

$$y' = 24x^3 + 22x$$

$$c) y = \frac{x \ln x}{x+1}$$

$$y' = \frac{(x \ln x)' \cdot (x+1) - (x \ln x) \cdot (x+1)'}{(x+1)^2}$$

$$y' = \frac{\left((x)' \cdot \ln x + x \cdot (\ln x)' \right) \cdot (x+1) - (x \ln x) \cdot \left((x)' + (1)' \right)}{(x+1)^2}$$

$$y' = \frac{\left(1 \cdot \ln x + x \cdot \frac{1}{x} \right) \cdot (x+1) - (x \ln x) \cdot 1}{(x+1)^2}$$

$$y' = \frac{(\ln x + 1) \cdot (x+1) - x \ln x}{(x+1)^2}$$

$$y' = \frac{x \ln x + \ln x + x + 1 - x \ln x}{(x+1)^2}$$

$$y' = \frac{\ln x + x + 1}{(x+1)^2}$$

$$\left(\frac{u}{v} \right)' = \frac{u' \cdot v - u \cdot v'}{v^2}$$

Zadaci za vježbu: Odrediti izvode sledećih funkcija

$$a) y = 5x^6 - 3x^5 + 4x - 8$$

$$b) y = 6\sqrt[3]{x} - 4\sqrt[4]{x}$$

$$c) y = (x^2 - 7) \cdot (x^2 + 6)$$

$$d) y = x^2 \cdot \cos x$$

$$e) y = \frac{x^2 - x + 1}{x^2 + 1}$$

$$f) y = \frac{\ln x}{x^2}$$

$$g) y = x \cdot \sin x + \cos x$$

$$h) y = (2 - x^2) \cdot \cos x + 2x \cdot \sin x$$

Uputstvo:
Koristiti tablicu
izvoda i osnovna
pravila izvoda.